

ABSTRACT

CHARACTERIZATION OF SUPPLEMENTS IN WEAKLY SUPPLEMENTED MODULES

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Let R Ring, M R -module, N, L and K are submodules of M R -module. N is called supplement of L in M if N is minimal in the set of submodules

$\{ K \subset M \mid L + K = M \}$, $L + N = M$ and $L \cap N \ll N$. Supplemented modules is module that every submodule has supplement. N is called weak supplement of L in M if $L + N = M$ and $L \cap N \ll M$. Weakly supplemented modules is module that every submodule has weak supplement.

In this research, we describe characterization weakly supplemented modules. For submodule $K \subset M$ that is weakly supplemented modules is supplement in M if and only if K is a *coclosed* submodule in M .

Key words : *module, supplement, weak supplement, coclosed submodule.*