

## ABSTRACT

### FACTORIZATION IN QUADRATIC FIELD $Q[\sqrt{d}]$

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For a square free integer  $d$  other than 1,

Let,

$$K = Q[\sqrt{d}] = \{x + y\sqrt{d} : x, y \in Q\}$$

This is called a quadratic field and it has degree 2 over  $Q$ . We will define a concept of “integer” for  $K$ , which will play the same role in  $K$  as the ordinary integers  $Z$  do in  $Q$ .

The integer of  $K$  are

$$\{a + b\sqrt{d} : a, b \in Z\} \text{ if } d \not\equiv 1 \pmod{4}$$

and

$$\{a + b\left(\frac{1+\sqrt{d}}{2}\right) : a, b \in Z\} \text{ if } d \equiv 1 \pmod{4}$$

For  $\alpha \in K$ , set  $Tr(\alpha) = \alpha + \bar{\alpha}$  and  $N(\alpha) = \alpha\bar{\alpha}$ . These are called the trace and norm of  $\alpha$ . We denote the integers of  $K$  as  $\mathcal{O}_K$ . Unique factorization in the integers of  $K$  does not always hold. The norm will play important role. If  $\alpha \in \mathcal{O}_K$  has norm which is prime in  $Z$ , then  $\alpha$  is irreducible in  $\mathcal{O}_K$ .

**Key Words** : square integer , quadratic field , integer of  $K$  , trace , norm , prime, irreducible.